

### UNIT-III

More Powerful LR parser (LR1, LALR) Using Armigers Grammars Equal Recovery in Lr parser Syntax Directed Transactions Definition, Evolution order of SDTS Application of SDTS. Syntax Directed Translation Schemes.

## UNIT-3

### CANONICAL LR PARSING

CLR refers to canonical lookahead. CLR parsing use the canonical collection of LR (1) items to build the CLR (1) parsing table. CLR (1) parsing table produces the more number of states as compare to the SLR (1) parsing.

In the CLR(1), we place

the reduce node only in the lookahead symbols. Various steps involved in the

CLR (1) Parsing:

- 1) For the given input string write a context free grammar
- 2) Check the ambiguity of the grammar
- 3) Add Augment production in the given grammar
- 4) Create Canonical collection of LR (0) items
- 5) Draw a data flow diagram (DFA)
- 6) Construct a CLR(1) parsing table

In the SLR method we were working with LR(0) items. In CLR parsing we will be using LR(1) items. LR(k) item is defined to be an item using lookaheads of length k. So, the LR(1) item is comprised of two parts: the LR(0) item and the lookahead associated with the item. The lookahead is used to determine that where we place the final item. The lookahead always add \$ symbol for the argument production.

LR(1) parsers are more powerful parser.

for LR(1) items we modify the Closure and GOTO function.

### Closure Operation

Closure(I)

repeat

for (each item  $A \rightarrow ?B?, a$  in I) for (each

production  $B \rightarrow ?$  in

$G'$ ) for (each terminal  $b$  in  $FIRST(?a)$ )

add  $[ B \rightarrow .?, b ]$  to set

I; until no more items are added to I; ret

urn I;

## GotoOperation

```
Goto(I,X)
Initialise J to be the empty set;
for( each item A ->?X?, a ] in I)
    Add item A ->?X?.?, a ] to set J; /* move the dot one
step */
return Closure(J); /* apply closure to the set */
```

## LR(1) items

```
Void items(G')
Initialise C to { closure ( {[S' -> .S,
$] } ) }; Repeat
    For( each set of items I in C)
        For( each grammar symbol X)
            if( GOTO(I, X) is not empty and not in
                C) Add GOTO(I, X) to C;
Until no new set of items are added to C;
```

## ALGORITHM FOR CONSTRUCTION OF THE CANONICAL LR PARSING TABLE

**Input:** grammar  $G'$

**Output:** canonical LR parsing table functions action and goto

1. Construct  $C = \{I_0, I_1, \dots, I_n\}$  the collection of sets of LR(1) items for  $G'$ . State  $i$  is constructed from  $I_i$ .
2. if  $[A \rightarrow a.ab, b >]$  is in  $I_i$  and  $\text{goto}(I_i, a) = I_j$ , then set  $\text{action}[i, a]$  to "shiftj". Here  $a$  must be a terminal.
3. if  $[A \rightarrow a., a]$  is in  $I_i$ , then set  $\text{action}[i, a]$  to "reduce  $A \rightarrow a$ " for all  $a$  in  $\text{FOLLOW}(A)$ . Here  $A$  may *not* be  $S'$ .
4. if  $[S' \rightarrow .S]$  is in  $I_i$ , then set  $\text{action}[i, \$]$  to "accept"
5. If any conflicting actions are generated by these rules, the grammar is not LR(1) and the algorithm fails to produce a parser.
6. The goto transitions for state  $i$  are constructed for all *nonterminals*  $A$  using the rule: If  $\text{goto}(I_i, A) = I_j$ , then  $\text{goto}[i, A] = j$ .
7. All entries not defined by rules 2 and 3 are made "error".
8. The initial state of the parser is the one constructed from the set of items containing  $[S' \rightarrow .S, \$]$ .

**Example,**

Consider the following grammar,

$S'' \rightarrow$   
 $SS$   
 $CCC$   
 $-$   
 $cCC$   
 $d$

Set of LR(1) items

**I0:**  $S'' \rightarrow$   
 $\cdot S, \$S$   
 $\cdot CC, \$$   
 $C \cdot$   
 $\cdot Cc, c/dC$   
 $\cdot d, c/d$

**I1:**  $S'' \rightarrow S \cdot, \$$

**I2:**  $S \rightarrow C \cdot C, \$$   
 $C \rightarrow \cdot Cc, \$$   
 $C \rightarrow \cdot d, \$$

**I3:**  $C \rightarrow c \cdot C, c/dC$   
 $\cdot Cc, c/dC$   
 $\cdot d, c/d$

**I4:**  $C \rightarrow d \cdot, c/d$

**I5:**  $S \rightarrow CC \cdot, \$$

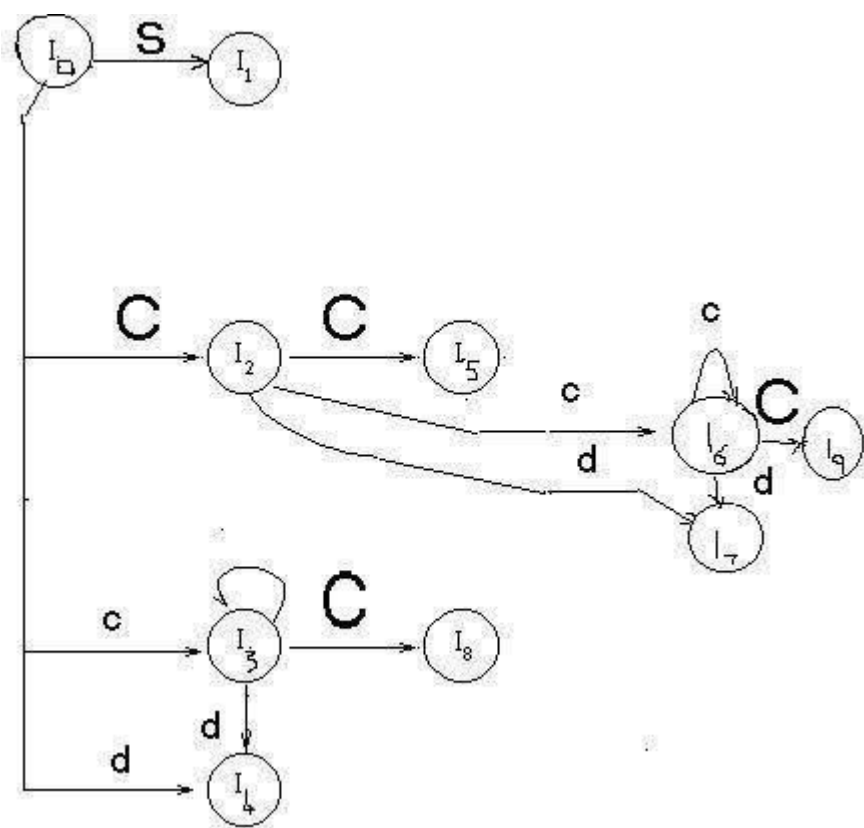
**I6:**  $C \rightarrow c \cdot C, \$$   
 $C \rightarrow \cdot cC, \$$   
 $C \rightarrow \cdot d, \$$

**I7:**  $C \rightarrow d \cdot, \$$

**I8:**  $C \rightarrow cC \cdot, c/d$

**I9:**  $C \rightarrow cC \cdot, \$$

Hereis whatthecorresponding DFAlooks like



Parsing Table:state	c	d	\$	S	C
0	S3	S4		1	2
1			acc		
2	S6	S7			5
3	S3	S4			8
4	R3	R3			
5			R1		
6	S6	S7			9
7			R3		
8	R2	R2			
9			R2		

## **.LALRPARSER:**

We begin with two observations. First, some of the states generated for LR(1) parsing have the same set of core (or first) components and differ only in their second component, the lookahead symbol. Our intuition is that we should be able to merge these states and reduce the number of states we have, getting close to the number of states that would be generated for LR(0) parsing. This observation suggests a hybrid approach: We can construct the canonical LR(1) sets of items and then look for sets of items having the same core. We merge these sets with common cores into one set of items. The merging of states with common cores can never produce a shift/reduce conflict that was not present in one of the original states because shift actions depend only on the core, not the lookahead. But it is possible for the merger to produce a reduce/reduce conflict.

Our second observation is that we are really only interested in the lookahead symbol in places where there is a problem. So our next thought is to take the LR(0) set of items and add lookaheads only where they are needed. This leads to a more efficient, but much more complicated method.

### **ALGORITHM FOR EASY CONSTRUCTION OF AN LALR TABLE**

Input:  $G'$

Output: LALR parsing table functions with action

and goto for  $G'$ . Method:

1. Construct  $C = \{I_0, I_1, \dots, I_n\}$  the collection of sets of LR(1) items for  $G'$ .
2. For each core present among the set of LR(1) items, find all sets having that core and replace these sets by the union.
3. Let  $C' = \{J_0, J_1, \dots, J_m\}$  be the resulting sets of LR(1) items. The parsing actions for state  $i$  are constructed from  $J_i$  in the same manner as in the construction of the canonical LR parsing table.
4. If there is a conflict, the grammar is not LALR(1) and the algorithm fails.
5. The goto table is constructed as follows: If  $J$  is the union of one or more sets of LR(1) items, that is,  $J = I_0 \cup I_1 \cup \dots \cup I_k$ , then the cores of  $\text{goto}(I_0, X)$ ,  $\text{goto}(I_1, X)$ , ...,  $\text{goto}(I_k, X)$  are the same, since  $I_0, I_1, \dots, I_k$  all have the same core. Let  $K$  be the union of all sets of items having the same core as  $\text{goto}(I_1, X)$ .

6. Thengoto(J,X)= K.  
**Consider the above example,**  
 I3&I6 can be replaced by their union I36:C->c.C,c/d/\$  
 C-  
 >.Cc,C/D/\$C  
 ->.d,c/d/\$  
 I47:C-  
 >d.,c/d/\$I89:C-  
 >Cc.,c/d/\$

**Parsing Table**

state	c	d	\$	S	C
0	S36	S47		1	2
1			Accept		
2	S36	S47			5
36	S36	S47			89
47	R3	R3			
5			R1		
89	R2	R2	R2		

**HANDLING ERRORS**  
 The LALR parser may continue to do reductions after the LR parser would have spotted an error, but the LALR parser will never do a shift after the point the LR parser would have discovered the error and will eventually find the error.

**DANGLING ELSE**  
 The dangling else is a problem in computer programming in which an optional else clause in an If-then(-else) statement results in nested conditionals being ambiguous. Formally, the context-free grammar of the language is ambiguous, meaning there is more than one correct parse tree.

In many programming languages one may write conditionally executed code in two forms: the if-then form, and the if-then-else form – the else clause is optional:

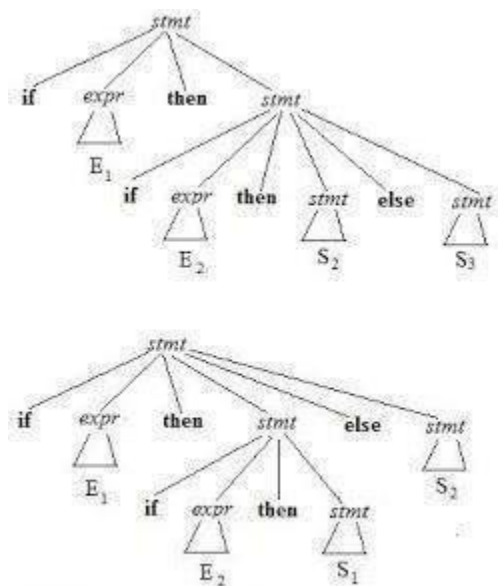


Fig 2.4 Two parse trees for an ambiguous sentence

Consider the grammar:

- S ::= E \$
- E ::= E + E
- | E \* E
- | ( E )
- | id
- | num

and four of its LALR(1) states:

I0: S ::= E \$           ?			
E ::= E + E + * \$	I1: S ::= E . \$	I2: E ::= E * . E	+ * \$
E ::= E * E + * \$	E ::= E . + E + * \$	E ::= E + E	+ * \$
E ::= ( E ) + * \$	E ::= E . * E + * \$	E ::= E * E	+ * \$
E ::= id + * \$		E ::= ( E )	+ * \$
E ::= num + * \$	I3: E ::= E * E .	+ * \$	E ::= id + * \$
	E ::= E . + E	+ * \$	E ::= num + * \$

$$E ::= E * E + * \$$$

Here we have a shift-reduce error. Consider the first two items in I3. If we have  $a*b+c$  and we have parsed  $a*b$ , do we reduce using  $E ::= E * E$  or do we shift more symbols? In the former case we get a parse tree  $(a*b)+c$ ; in the latter case we get  $a*(b+c)$ . To resolve this conflict, we can specify that  $*$  has higher precedence than  $+$ . The precedence of a grammar production is equal to the precedence of the rightmost token at the rhs of the production. For example, the precedence of the production  $E ::= E * E$  is equal to the precedence of the operator  $*$ , the precedence of the production  $E ::= ( E )$  is equal to the precedence of the token  $)$ , and the precedence of the production  $E ::= \text{if } E \text{ then } E \text{ else } E$  is equal to the precedence of the token  $\text{else}$ . The idea is that if the look ahead has higher precedence than the production currently used, we shift. For example, if we are parsing  $E+E$  using the production rule  $E ::= E+E$  and the look ahead is  $*$ , we shift  $*$ . If the look ahead has the same precedence as that of the current production and is left associative, we reduce, otherwise we shift. The above grammar is valid if we define the precedence and associativity of all the operators. Thus, it is very important when you write a parser using CUP or any other LALR(1) parser generator to specify associativities and precedence for most tokens (especially for those used as operators). Note: you can explicitly define the precedence of a rule in CUP using the %prec directive:

$E ::= \text{MINUS } E \% \text{prec UMINUS}$

where UMINUS is a pseudo-token that has higher precedence than TIMES, MINUS etc, so that  $-1*2$  is equal to  $(-1)*2$ , not to  $-(1*2)$ .

Another thing we can do when specifying an LALR(1) grammar for a parser generator is error recovery. All the entries in the ACTION and GOTO tables that have no content correspond to syntax errors. The simplest thing to do in case of an error is to report it and stop the parsing. But we would like to continue parsing finding more errors. This is called *error recovery*. Consider the grammar:

$S ::= L = E ;$

$\{ SL \}$   
;error ;

$SL ::= S ;$

$\{ SLS \}$

The special token error indicates to the parser what to do in case of invalid syntax for S (an invalid statement). In this case, it reads all the tokens from the input stream until it finds the first semicolon. The way the parser handles this is to first push an error state in the stack. In case of an error, the parser pops out elements from the stack until it finds an error state where it can proceed. Then it discards tokens from the input until a restart is possible. Inserting error handling productions in the proper places in a grammar to do good error recovery is considered very hard.

## LR ERROR RECOVERY

An LR parser will detect an error when it consults the parsing action table and finds a blank or error entry. Errors are never detected by consulting the goto table. An LR parser will detect an error as soon as there is no valid continuation for the portion of the input thus far

scanned. A canonical LR parser will not make even a single reduction before announcing the error. SLR and LALR parsers may make several reductions before detecting an error, but they will never shift an erroneous input symbol onto the stack.

**PANIC-MODE ERROR RECOVERY**

We can implement panic-mode error recovery by scanning down the stack until a state *s* with a goto on a particular nonterminal *A* is found. Zero or more input symbols are then discarded until a symbol *a* is found that can legitimately follow *A*. The parser then pushes the state GOTO(*s*, *A*) and resumes normal parsing. The situation might exist where there is more than one choice for the nonterminal *A*. Normally these would be nonterminals representing major program pieces, e.g. an expression, a statement, or a block. For example, if *A* is the nonterminal *stmt*, *a* might be semicolon or *}*, which marks the end of a statement sequence. This method of error recovery attempts to eliminate the phrase containing the syntactic error. The parser determines that a string derivable from *A* contains an error. Part of that string has already been processed, and the result of this processing is a sequence of states on top of the stack. The remainder of the string is still in the input, and the parser attempts to skip over the remainder of this string by looking for a symbol on the input that can legitimately follow *A*. By removing states from the stack, skipping over the input, and pushing GOTO(*s*, *A*) on the stack, the parser pretends that it has found an instance of *A* and resumes normal parsing.

**PHRASE-LEVEL RECOVERY**

Phrase-level recovery is implemented by examining each error entry in the LR action table and deciding on the basis of language usage the most likely programmer error that would give rise to that error. An appropriate recovery procedure can then be constructed; presumably the top of the stack and/or first input symbol would be modified in a way deemed appropriate for each error entry. In designing specific error-handling routines for an LR parser, we can fill in each blank entry in the action field with a pointer to an error routine that will take the appropriate action selected by the compiler designer.

The actions may include insertion or deletion of symbols from the stack or the input or both, or alteration and transposition of input symbols. We must make our choices so that the LR parser will not get into an infinite loop. A safe strategy will assure that at least one input symbol will be removed or shifted eventually, or that the stack will eventually shrink if the end of the input has been reached. Popping a stack state that covers a non terminal should be avoided, because this modification eliminates from the stack a construct that has already been successfully parsed.

**Syntax Directed Translations**

We associate information with a language construct by attaching attributes to the grammar symbol(s) representing the construct. A syntax-directed definition specifies the values of attributes by associating semantic rules with the grammar productions. For example, an infix-to-postfix translator might have a production and rule

PRODUCTION	SEMANTIC RULE
$E \rightarrow E_1 + T$	$E.code = E_1.code \parallel T.code \parallel '+'$

This production has two nonterminals, E and T; the subscript in E<sub>1</sub> distinguishes the occurrence of E in the production body from the occurrence of E as the head. Both E and T have a string-valued attribute `code`. The semantic rule specifies that the string `E.code` is formed by concatenating `Ei.code`, `T.code`, and the character '+'. While the rule makes it explicit that the translation of E is built up from the translations of E<sub>1</sub>, T, and '+', it may be inefficient to implement the translation directly by manipulating strings.

as syntax-directed translation schemes embed program fragments called semantic actions within production bodies

There are two notations for attaching semantic rules:

1. **Syntax Directed Definitions.** High-level specification hiding many implementation details (also called **Attribute Grammars**).
2. **Translation Schemes.** More implementation oriented: Indicate the order in which semantic rules are to be evaluated.

### Syntax Directed Definitions

Syntax Directed Definitions are a generalization of context-free grammars in which:

1. Grammar symbols have an associated set of **Attributes**;
2. Productions are associated with **Semantic Rules** for computing the values of attributes. Such formalism generates **Annotated Parse-Trees** where each node of the tree is a record with a field for each attribute (e.g., `X.a` indicates the attribute `a` of the grammar symbol `X`).

The value of an attribute of a grammar symbol at a given parse-tree node is defined by a semantic rule associated with the production used at that node.

We distinguish between two kinds of attributes:

1. **Synthesized Attributes.** They are computed from the values of the attributes of the children nodes.
2. **Inherited Attributes.** They are computed from the values of the attributes of both the siblings and the parent nodes

SyntaxDirectedDefinitions:AnExample

LetusconsidertheGrammarforarithmeticexpressions.TheSyntaxDirectedDefinitiona ssociates to eachnon terminal asynthesized attributecalledval.

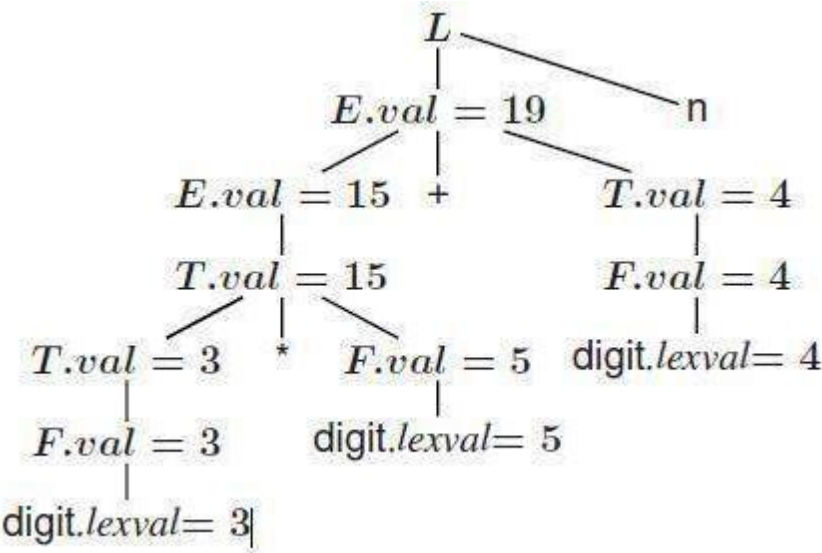
PRODUCTION	SEMANTIC RULE
$E \rightarrow E_1 + T$	$E.code = E_1.code \parallel T.code \parallel '+'$
$F \rightarrow (E)$	$F.val := E.val$
$F \rightarrow digit$	$F.val := digit.lexval$

SDDofasimpledeskcalculator

S-ATTRIBUTEDDEFINITIONS

**Definition.** An **S-Attributed Definition** is a Syntax Directed Definition that usesonlysynthesized attributes.

- **Evaluation Order.** Semantic rules in a S-Attributed Definition canbeevaluatedby abottom-up,orPostOrder, traversal oftheparse-tree.
- **Example.** The above arithmetic grammar is an example of an S-AttributedDefinition.Theannotatedparse-treefortheinput3\*5+4nis:



## L-attributed definition

**Definition:** A SDT is *L-attributed* if each inherited attribute of  $X_i$  in the RHS of  $A \rightarrow X_1 X_2 \dots X_n$ :

$X_i$  depends only on

1. attributes of  $X_1 X_2 \dots X_{i-1}$  (symbols to the left of  $X_i$  in the RHS)
2. inherited attributes of  $A$ .

## Restrictions for translation schemes:

1. Inherited attribute of  $X_i$  must be computed by an action before  $X_i$ .
2. An action must not refer to synthesized attribute of any symbol to the right of that action.
3. Synthesized attribute for  $A$  can only be computed after all attributes it references have been completed (usually at end of RHS).

## Evaluation order of SDTs

1 Dependency Graphs

2 Ordering the Evaluation of Attributes

3 S-Attributed Definitions

4 L-Attributed Definitions

"Dependency graphs" are a useful tool for determining an evaluation order for the attribute instances in a given parse tree. While an annotated parse tree shows the values of attributes, a dependency graph helps us determine how those values can be computed.

## 1 Dependency Graphs

A *dependency graph* depicts the flow of information among the attribute instances in a particular parse tree; an edge from one attribute instance to another means that the value of the first is needed to compute the second. Edges express constraints implied by the semantic rules. In more detail:

Suppose that a semantic rule associated with a production  $p$  defines the value of inherited attribute  $B.c$  in terms of the value of  $X.a$ . Then, the dependency graph has an edge from  $X.a$  to  $B.c$ . For each node  $N$  labeled  $B$  that corresponds to an occurrence of this  $B$  in the body of production  $p$ , create an edge to attribute  $c$  at  $N$  from the attribute  $a$  at the node  $M$  that corresponds to this occurrence of  $X$ . Note that  $M$  could be either the parent or a sibling of  $N$ .

Since a node  $N$  can have several children labeled  $X$ , we again assume that subscripts distinguish among uses of the same symbol at different places in the production.

**Example:** Consider the following production and rule:

#### PRODUCTION

$$E \rightarrow E_1 + T$$

#### SEMANTIC RULE

$$E.val = E_1.val + T.val$$

At every node  $N$  labeled  $E$ , with children corresponding to the body of this production, the synthesized attribute  $val$  at  $N$  is computed using the values of  $val$  at the two children, labeled  $E_1$  and  $T$ . Thus, a portion of the dependency graph for every parse tree in which this production is used looks like Fig. 5.6. As a convention, we shall show the parse tree edges as dotted lines, while the edges of the dependency graph are solid.

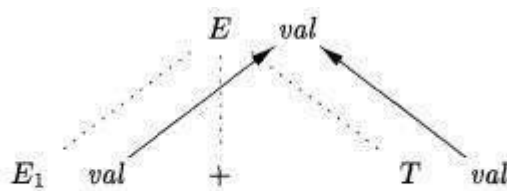


Figure 5.6:  $E.val$  is synthesized from  $E_1.val$  and  $E_2.val$

## 2. Ordering the Evaluation of Attributes

The dependency graph characterizes the possible orders in which we can evaluate the attributes at the various nodes of a parse tree. If the dependency graph has an edge from node  $M$  to node  $N$ , then the attribute corresponding to  $M$  must be evaluated before the attribute of  $N$ . Thus, the only allowable orders of evaluation are those sequences of nodes  $N_1, N_2, \dots, N_k$  such that if there is an edge of the dependency graph from  $N_i$  to  $N_j$ , then  $i < j$ . Such an ordering embeds a directed graph into a linear order, and is called a topological sort of the graph.

If there is a cycle in the graph, then there are no topological sorts; that is, there is no way to evaluate the SDD on this parse tree. If there are no cycles, however, then there is always at least one topological sort.

## 3. S-Attributed Definitions

An SDD is *S-attributed* if every attribute is synthesized. When an SDD is S-attributed, we can evaluate its attributes in any bottom-up order of the nodes of the parse tree. It is often especially simple to evaluate the attributes by performing a postorder traversal of the parse tree and evaluating the attributes at a node  $N$  when the traversal leaves  $N$  for the last time.

S-attributed definitions can be implemented during bottom-up parsing, since a bottom-up parse corresponds to a postorder traversal. Specifically, postorder corresponds exactly to the order in which an LR parser reduces a production body to its head.

## 4. L-Attributed Definitions

The idea behind this class is that, between the attributes associated with a production body, dependency-graph edges can go from left to right, but not from right to left (hence "L-attributed"). More precisely, each attribute must be either

1. Synthesized, or
2. Inherited, but with the rules limited as follows. Suppose that there is a production  $A \rightarrow X_1 X_2 \dots X_n$ , and that there is an inherited attribute  $X_i$  computed by a rule associated with this production.

Then the rule may use only:  
 Inherited attributes associated with the head A.  
 Either inherited or synthesized attributes associated with the occurrences of symbols  $X_1, X_2, \dots, X_{(i-1)}$  located to the left of  $X_i$ .  
 Inherited or synthesized attributes associated with this occurrence of  $X_i$  itself, but only in such a way that there are no cycles in a dependency graph formed by the attributes of this  $X_i$

## Application of SDTS

### 1 Construction of Syntax Trees The Structure of a Type

The main application is the construction of syntax trees. Since some compilers use syntax trees as an intermediate representation, a common form of SDD turns its input string into a tree. To complete the translation to intermediate code, the compiler may then walk the syntax tree, using another set of rules that are in effect an SDD on the syntax tree rather than the parse tree.

### 1 Construction of Syntax Trees

Each node in a syntax tree represents a construct; the children of the node represent the meaningful components of the construct. A syntax-tree node representing an expression  $E_1 + E_2$  has label  $+$  and two children representing the subexpressions  $E_1$  and  $E_2$ .  
 We implement the nodes of a syntax tree by objects with a suitable number of fields. Each object will have an *op* field that is the label of the node.  
 The objects will have additional fields as follows:

- If the node is a leaf, an additional field holds the lexical value for the leaf. A constructor function `Leaf(op, val)` creates a leaf object. Alternatively, if nodes are reviewed as records, then `Leaf` returns a pointer to a new record for a leaf.
- If the node is an interior node, there are as many additional fields as the node has children in the syntax tree. A constructor function `Node` takes two or more arguments: `Node(op, c1, c2, ..., ck)` creates an object with first field *op* and *k* additional fields for the children  $c_1, \dots, c_k$ .

Example

PRODUCTION	SEMANTIC RULES
1) $E \rightarrow E_1 + T$	$E.node = \text{new Node}('+', E_1.node, T.node)$
2) $E \rightarrow E_1 - T$	$E.node = \text{new Node}('-', E_1.node, T.node)$
3) $E \rightarrow T$	$E.node = T.node$
4) $T \rightarrow ( E )$	$T.node = E.node$
5) $T \rightarrow \text{id}$	$T.node = \text{new Leaf}(\text{id}, \text{id.entry})$
6) $T \rightarrow \text{num}$	$T.node = \text{new Leaf}(\text{num}, \text{num.val})$

Figure 5.10: Constructing syntax trees for simple expressions

Figure 5.1 1 shows the construction of a syntax tree for the input  $a - 4 + c$ . The nodes of the syntax tree are shown as records, with the *op* field first. Syntax-tree edges are now shown as solid lines. The underlying parse tree, which need not actually be constructed, is shown with dotted edges. The

third type of line, shown dashed, represents the values of *E.node* and *T.node*; each line points to the appropriate syntax-tree node.

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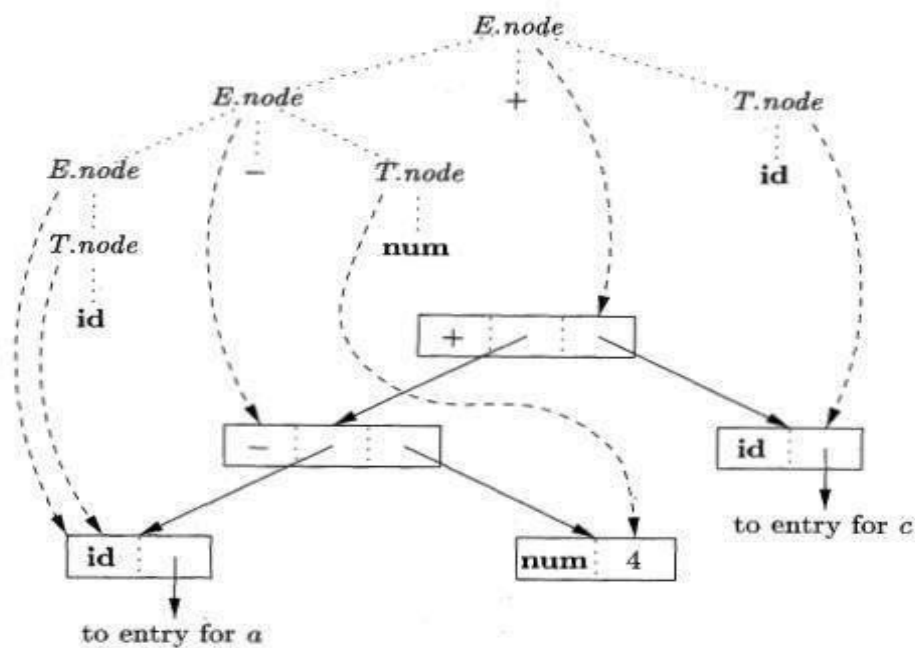


Figure 5.11: Syntax tree for  $a - 4 + c$

- 1)  $p_1 = \text{new Leaf}(\text{id}, \text{entry-}a);$
- 2)  $p_2 = \text{new Leaf}(\text{num}, 4);$
- 3)  $p_3 = \text{new Node}('-', p_1, p_2);$
- 4)  $p_4 = \text{new Leaf}(\text{id}, \text{entry-}c);$
- 5)  $p_5 = \text{new Node}('+', p_3, p_4);$

Figure 5.12: Steps in the construction of the syntax tree for  $a - 4 + c$

## 2 The Structure of a Type

The type `int [2][3]` can be read as, "array of 2 arrays of 3 integers." The corresponding type expression `array(2, array(3, integer))` is represented by the tree in Fig. 5.15. The operator `array` takes two parameters, a number and a type. If types are represented by trees, then this operator returns a tree node labeled `array` with two children for a number and a type.

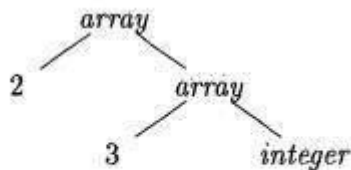


Figure 5.15: Type expression for `int[2][3]`

Nonterminal *B* generates one of the basic types **int** and **float**. *T* generates a basic type when *T* derives *BC* and *C* derives *e*. Otherwise, *C* generates array components consisting of a sequence of integers, each integer surrounded by brackets.

PRODUCTION	SEMANTIC RULES
$T \rightarrow B C$	$T.t = C.t$ $C.b = B.t$
$B \rightarrow \text{int}$	$B.t = \text{integer}$
$B \rightarrow \text{float}$	$B.t = \text{float}$
$C \rightarrow [\text{num}] C_1$	$C.t = \text{array}(\text{num.val}, C_1.t)$ $C_1.b = C.b$
$C \rightarrow \epsilon$	$C.t = C.b$

Figure 5.16:  $T$  generates either a basic type or an array type

An annotated parse tree for the input string `int [ 2 ] [ 3 ]` is shown in Fig. 5.17. The corresponding type expression in Fig. 5.15 is constructed by passing the type *integer* from  $B$ , down the chain of  $C$ 's through the inherited attribute  $b$ . The array type is synthesized up the chain of  $C$ 's through the attribute  $t$ .

In more detail, at the root for  $T \rightarrow B C$ , nonterminal  $C$  inherits the type from  $B$ , using the inherited attribute  $C.b$ . At the rightmost node for  $C$ , the production is  $C \rightarrow \epsilon$ , so  $C.t$  equals  $C.b$ . The semantic rules for the production  $C \rightarrow [\text{num}] C_1$  form  $C.t$  by applying the operator `array` to the operands `num.val` and  $C_1.t$ .

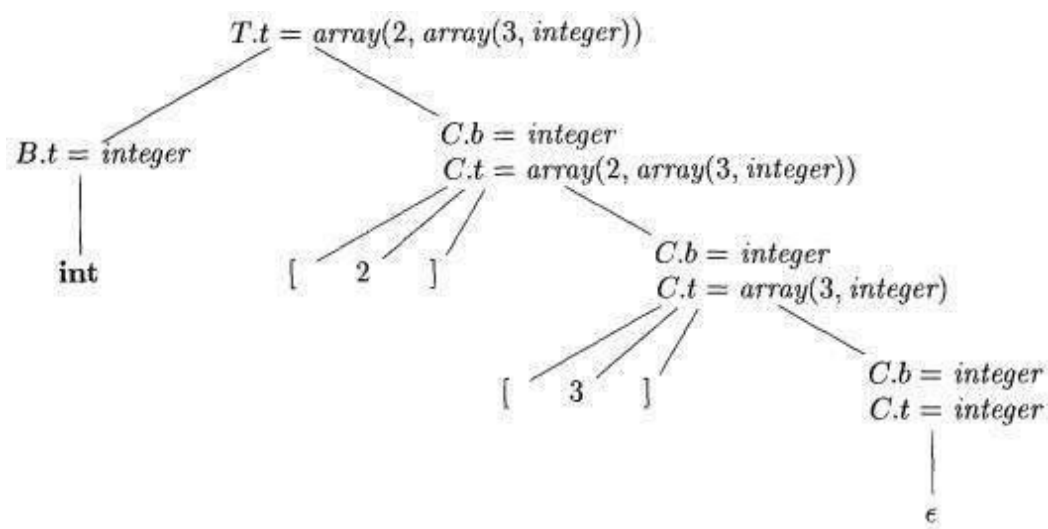


Figure 5.17: Syntax-directed translation of array types

SyntaxDirectedTranslationSchemes.

- 1Postfix Translation Schemes
- 2 Parser-Stack Implementation of Postfix
- SDT's3SDT's WithActions InsideProductions
- 4EliminatingLeftRecursion FromSDT's

*syntax-directed translation scheme* (SDT) is a context-free grammar with program fragments embedded within production bodies. The program fragments are called *semantic actions* and can appear at any position within a production body. By convention, we place curly braces around actions; if braces are needed as grammar symbols, then we quote them. SDT's are implemented during parsing, without building a parse tree.

Two important classes of SDD's are

- 1. The underlying grammar is LR-parsable, and the SDD is S-attributed.
- 2. The underlying grammar is LL-parsable, and the SDD is L-attributed.

1PostfixTranslationSchemes

simplest SDD implementation occurs when we can parse the grammar bottom-up and the SDD is S-attributed. In that case, we can construct an SDT in which each action is placed at the end of the production and is executed along with the reduction of the body to the head of that production. SDT's with all actions at the right ends of the production bodies are called postfix SDT's.

Example 5.14 : The postfix SDT in Fig. 5.18 implements the desk calculator SDD of Fig. 5.1, with one change: the action for the first production prints a value. The remaining actions are exact counterparts of the semantic rules. Since the underlying grammar is LR, and the SDD is S-attributed, these actions can be correctly performed along with the reduction steps of the parser.

$L$	$\rightarrow$	$E n$	$\{ \text{print}(E.val); \}$
$E$	$\rightarrow$	$E_1 + T$	$\{ E.val = E_1.val + T.val; \}$
$E$	$\rightarrow$	$T$	$\{ E.val = T.val; \}$
$T$	$\rightarrow$	$T_1 * F$	$\{ T.val = T_1.val \times F.val; \}$
$T$	$\rightarrow$	$F$	$\{ T.val = F.val; \}$
$F$	$\rightarrow$	$( E )$	$\{ F.val = E.val; \}$
$F$	$\rightarrow$	<b>digit</b>	$\{ F.val = \text{digit.lexval}; \}$

Figure 5.18: Postfix SDT implementing the desk calculator

2Parser-StackImplementationofPostfixSDT's

The attribute(s) of each grammar symbol can be put on the stack in a place where they can be found during the reduction. The best plan is to place the attributes along with the grammar symbols (or the LR states that represent these symbols) in records on the stack itself. In Fig. 5.19, the parser stack contains records with a field for a grammar symbol (or parser state) and, below it, a field for an attribute. The three grammar symbols XYZ are on top of the stack; perhaps they

are about to be reduced according to a production like  $A \rightarrow X YZ$ . Here, we show  $X.x$  as the one attribute of  $X$ , and so on. In general, we can allow for more attributes, either by making the records large enough or by putting pointers to records on the stack. With small attributes, it may be simpler to make the records large enough, even if some fields go unused some of the time. However, if one or more attributes are of unbounded size — say, they are character strings — then it would be better to put a pointer to the attribute's value in the stack record and store the actual value in some larger, shared storage area that is not part of the stack.

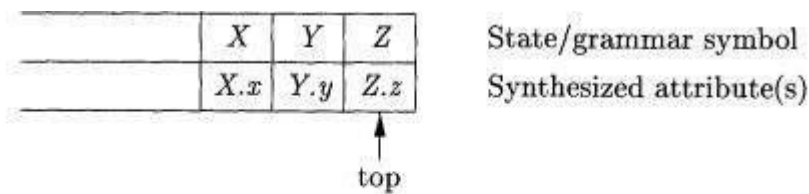


Figure 5.19: Parser stack with a field for synthesized attributes

### 3 SDT's With Actions Inside Productions

An action may be placed at any position within the body of a production. It is performed immediately after all symbols to its left are processed. Thus, if we have a production  $B \rightarrow X \{a\} Y$ , the action  $a$  is done after we have recognized  $X$  (if  $X$  is a terminal) or all the terminals derived from  $X$  (if  $X$  is a nonterminal).

More precisely,

- If the parse is bottom-up, then we perform action  $a$  as soon as this occurrence of  $X$  appears on the top of the parsing stack.
- If the parse is top-down, we perform  $a$  just before we attempt to expand this occurrence of  $Y$  (if  $Y$  is a nonterminal) or check for  $Y$  on the input (if  $Y$  is a terminal).

### 4 Eliminating Left Recursion From SDT's

First, consider the simple case, in which the only thing we care about is the order in which the actions in an SDT are performed. For example, if each action simply prints a string, we care only about the order in which the strings are printed. In this case, the following principle can guide us:

When transforming the grammar, treat the actions as if they were terminal symbols.

This principle is based on the idea that the grammar transformation preserves the order of the terminals in the generated string. The actions are therefore executed in the same order in any left-to-right parse, top-down or bottom-up.

The "trick" for eliminating left recursion is to take two productions

$$A \rightarrow Aa|b$$

that generate strings consisting of a  $b^j$  and any number of  $a$ 's, and replace them by productions that generate the same strings using a new nonterminal  $R$  (for "remainder") of the first production:

$$A \rightarrow bR$$

$$R \rightarrow \bullet aR | \epsilon$$

If  $\beta$  does not begin with  $A$ , then  $A$  no longer has a left-recursive production. In regular-definition terms, with both sets of productions,  $A$  is defined by  $\theta(A)^*$ .

**Example 5.17:** Consider the following E-productions from an SDT for translating infix expressions into postfix notation:

$$E \rightarrow E_1 + T \{ \text{print}(' + '); \} E_2$$

$$E \rightarrow T$$

If we apply the standard transformation to  $E$ , the remainder of the left-recursive production is a

$$= E_1 + T \{ \text{print}(' + '); \}$$

and the body of the other production is  $T$ . If we introduce  $R$  for the remainder of  $E$ , we get the set of productions:

$$E \rightarrow TR$$

$$R \rightarrow E_1 + T \{ \text{print}(' + '); \}$$

$$R \rightarrow e$$

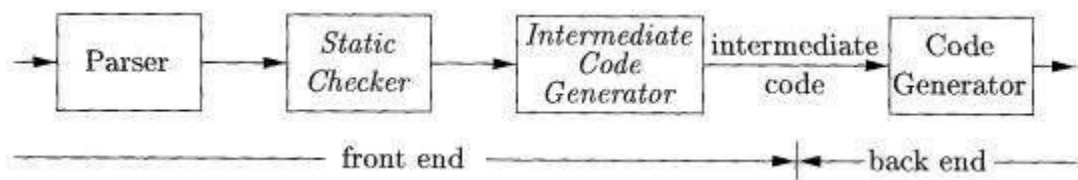
When the actions of an SDD compute attributes rather than merely printing output, we must be more careful about how we eliminate left recursion from a grammar. However, if the SDD is S-attributed, then we can always construct an SDT by placing attribute-computing actions at appropriate positions in the new productions.

**UNIT-III**  
Intermediated Code: Generation Variantsof Syntaxtrees3 Addresscode, TypesandDeceleration, Translationof Expressions, TypeChecking. CantedFlowBackpatching?

**INTERMEDIATECODE**

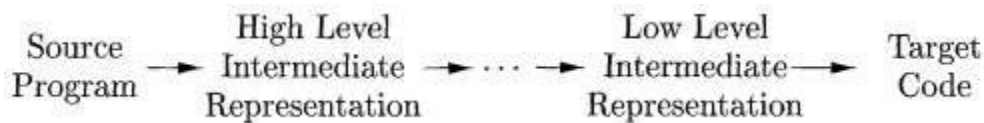
Intheanalysis-synthesismodelofacompiler,thefrontendanalyzesasourceprogram and creates an intermediate representation, from which the back end generates targetcode. This facilitates *retargeting*: enables attaching a back end for the new machine to anexistingfront end.

**LogicalStructureofa CompilerFrontEnd**



Acompilerfrontendisorganizedasinfigureabove,whereparsing,staticchecking, and intermediate-code generation are done sequentially; sometimes they can becombined and folded into parsing. All schemes can be implemented by creating a syntaxtreeand traversing the tree.

Static checking includes *type checking*, which ensures that operators are applied to compatibleoperands.Intheprocessoftranslatingaprogram inagiven sourcelanguageintocodefor agiventargetmachine,a compilerconstruct a sequenceofintermediate representations



**Sequenceofintermediaterepresentations**

High-levelrepresentationsareclosetothsourcelanguageandlow-levelrepresentationsareclosetothe target machine. A low-level representation is suitable for machine-dependent tasks like registerallocationand instruction selection.

JSVGKrishna,AssociateProfessor.

VariantsofSyntax Trees

- 1 DirectedAcyclicGraphsforExpressions
- 2 TheValue-NumberMethod forConstructing DAG's

1.DirectedAcyclicGraphsforExpressions

Like the syntax tree for an expression, a DAG has leaves corresponding to atomicoperands and interior codes corresponding to operators. The difference is that a node *N* in a DAG hasmore than one parent if *N* represents a com-mon subexpression; in a syntax tree, the tree for thecommon subexpression would be replicated as many times as the subexpression appears in the originalexpression.

**Example:**Considerexpression  
 $a + a * (b - c) + (b - c) * d$

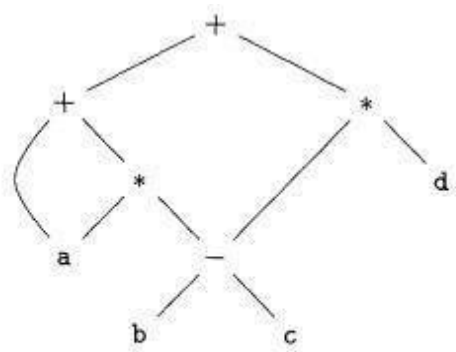


Figure 6.3: Dag for the expression  $a + a * (b - c) + (b - c) * d$

2TheValue-NumberMethodforConstructingDAG's

The nodes of a syntax tree or DAG are stored in an array of records, as suggested by Fig. 6.6.Each row of the array represents one record, and therefore one node. In each record, the first field is anoperation code, indicating the label of the node. In Fig. 6.6(b), leaves have one additional field, whichholds the lexical value (either a symbol-table pointer or a constant, in this case), and interior nodes havetwoadditional fields indicating the left andright children.

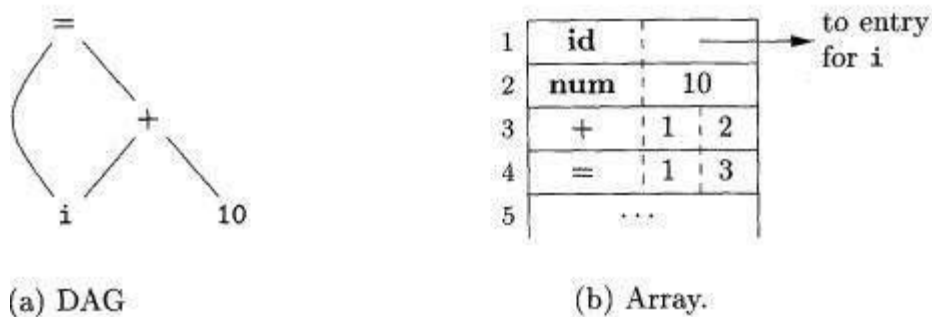


Figure 6.6: Nodes of a DAG for  $i = i + 10$  allocated in an array

In this array, we refer to nodes by giving the integer index of the record for that node within the array. This integer is called the value number for the node.

**Algorithm:** The value-number method for constructing the nodes of

a DAG. INPUT: Label op, node l, and node r.

OUTPUT: The value number of a node in the array with signature (op, l, r).

METHOD : Search the array for a node M with label op, left child l, and right child r. If there is such a node, return the value number of M. If not, create in the array a new node N with label op, left child l, and right child r, and return its value number.

### Three-Address Code

1 Addresses and

Instructions 2 Quadruples

3 Triples

In three-address code, there is at most one operator on the right side of an instruction; that is, no built-up arithmetic expressions are permitted. Thus a source-language expression like  $x + y * z$  might be translated into the sequence of three-address instructions

$$\begin{aligned}t_1 &= y * z \\t_2 &= x + t_1\end{aligned}$$

where  $t_1$  and  $t_2$  are compiler-generated temporary names.

#### 1 Addresses and Instructions

An address can be one of the following:

- *A name.* Source-program names to appear as addresses in three-address code. In an implementation, a source name is replaced by a pointer to its symbol-table entry, where all information about the name is kept.
- *A constant.* A compiler must deal with many different types of constants and variables.
- *A compiler-generated temporary.* Useful in optimizing compilers, to create a distinct name each time a temporary is needed. These temporaries can be combined, if possible, when registers are allocated to variables.

#### common three-address instruction

**1. Assignment Statement:**  $x = y \text{ op } z$  and  $x = \text{op } y$

Here,  $x$ ,  $y$  and  $z$  are the operands.  $\text{op}$  represents the operator.

**2. Copy Statement:**  $x = y$

**3. Conditional Jump:** If  $x \text{ rel op } y$  goto  $X$

If the condition “ $x \text{ rel op } y$ ” gets **satisfied**, then-

The control is sent directly to the location specified by label  $X$ . All the statements in between are skipped.

If the condition “ $x \text{ rel op } y$ ” **fails**, then-

The control is not sent to the location specified by label  $X$ .

The next statement appearing in the usual sequence is executed.

#### 4. Unconditional Jump-goto $X$

On executing the statement, The control is sent directly to the location specified by label  $X$ .

All the statements in between are skipped.

#### 5. Procedure Call-param $x$ call pre return $y$

Here,  $p$  is a function which takes  $x$  as a parameter and returns  $y$ .  
For a procedure call  $p(x_1, \dots, x_n)$

param  $x_1$

...

param  $x_n$

call  $p, n$

#### 6. Indexed copy instructions: $x = y[i]$ and $x[i] = y$

Left: sets  $x$  to the value in the location  $i$  memory units beyond

$y$  Right: sets the contents of the location  $i$  memory units beyond  $x$  to  $y$

#### 7. Address and pointer instructions:

$x = \&y$  sets the value of  $x$  to be the location (address) of  $y$ .

$x = *y$ , presumably  $y$  is a pointer or temporary whose value is a location. The value of  $x$  is set to the contents of that location.

$*x = y$  sets the value of the object pointed to by  $x$  to the value of  $y$ .

### Data Structure

Three address code is represented as record structure with fields for operator and operands. These records can be stored as array or linked list. Most common implementations of three address code are Quadruples, Triples and Indirect triples.

#### 2. Quadruples

Quadruples consists of four fields in the record structure. One field to store operator  $op$ , two fields to store operands or arguments  $arg_1$  and  $arg_2$  and one field to store result  $res$ .

$res = arg_1 \ op$

$arg_2$  Example:  $a = b + c$

$b$  is represented as  $arg_1$ ,  $c$  is represented as  $arg_2$ ,  $+$  as  $op$  and  $a$  as  $res$ .

Unary operators like „-,„do not use agr2. Operators like param do not use agr2 nor result. Forconditional and unconditional statements res is label. Arg1, arg2 and res are pointers tosymboltable orliteral table for thenames.

Example:a =-b \*d+c +(-b)\* d

Three address code for the above statement is as followst1 =-b

t2 = t1 \*

dt3 = t2 +

ct4 =-b

t5 = t4 \* d

t6 = t3 +

t5a=t6

Quadruplesfortheabove exampleis asfollows

Op	Arg1	Arg2	Res
-	B		t1
*	t1	d	t2
+	t2	c	t3
-	B		t4
*	t4	d	t5
+	t3	t5	t6
=	t6		a

### 3TRIPLES

Triples uses only three fields in the record structure. One field for operator, two fields for operands named as arg1 and arg2. Value of temporary variable can be accessed by the position of the statement the computes it and not by location as in quadruples.

Example:  $a = -b * d + c + (-b) * d$

Triples for the above example is as follows

Stmt no	Op	Arg1	Arg2
(0)	-	b	
(1)	*	d	(0)
(2)	+	c	(1)
(3)	-	b	
(4)	*	d	(3)
(5)	+	(2)	(4)
(6)	=	a	(5)

Arg1 and arg2 may be pointer to symbol table for program variables or literal table for constant or pointers into triple structure for intermediate results.

Example: Triples for statement  $x[i] = y$  which generate two records is as follows

Stmt no	Op	Arg1	Arg2
(0)	$[] =$	x	i
(1)	=	(0)	y

Triples for statement  $x = y[i]$  which generate test two records is as follows

Stmt no	Op	Arg1	Arg2
(0)	=[]	y	i
(1)	=	x	(0)

Triples are alternative ways for representing syntax tree or Directed acyclic graph for program defined names.

**Indirect Triples**

Indirect triples are used to achieve indirection in listing of pointers. That is, it uses pointer to triples than listing of triples themselves.

Example:  $a = -b * d + c + (-b) * d$

	Stmt no	Stmt no	Op	Arg1	Arg2
(0)	(10)	(10)	-	b	
(1)	(11)	(11)	*	d	(0)
(2)	(12)	(12)	+	c	(1)
(3)	(13)	(13)	-	b	
(4)	(14)	(14)	*	d	(3)
(5)	(15)	(15)	+	(2)	(4)
(6)	(16)	(16)	=	a	(5)

## Types and Declarations

- 1 *Type Expressions*
- 2 *Type Equivalence*
- 3 *Declarations*
- 4 *Storage Layout for Local Names*

### 1 Type Expressions

Types have structure, which we shall represent using *type expressions*: a type expression is either a basic type or is formed by applying an operator called a *type constructor* to a type expression.

#### Definition

- A basic type is a type expression. Typical basic types for a language include *boolean*, *char*, *integer*, *float*, and *void*; the latter denotes "the absence of a value."
- A type name is a type expression.
- A type expression can be formed by applying the array type constructor to a number and a type expression.
- A record is a data structure with named fields. A type expression can be formed by applying the *record* type constructor to the field names and their types.
- If  $s$  and  $t$  are type expressions, then their Cartesian product  $s \times t$  is a type expression. Products are introduced for completeness; they can be used to represent a list or tuple of types (e.g., for function parameters).
- Type expressions may contain variables whose values are type expressions

### 2 Type Equivalence

Many type-checking rules have the form, "if two type expressions are equal then return a certain type else error." Potential ambiguities arise when names are given to type expressions. The key issue is whether a name in a type expression stands for itself or whether it is an abbreviation for another type expression.

Since type names denote type expressions, they can set up implicit cycles; see the box on "Type Names and Recursive Types." If edges to type names are redirected to the type expressions denoted by the names, then the resulting graph can have cycles due to recursive types.

When type expressions are represented by graphs, two types are *structurally equivalent* if and only if one of the following conditions is true:

They are the same basic type.

They are formed by applying the same constructor to structurally equivalent types. One is a type name that denotes the other.

If type names are treated as standing for themselves, then the first two conditions in the above definition lead to *name equivalence* of type expressions.

Name-equivalent expressions are assigned the same value number. Structural equivalence can be tested using the unification algorithm.

### 3. Declarations

Understand types and declarations using a simplified grammar that declares just one name at a time; The grammar is

$$\begin{aligned} D &\rightarrow T \text{ id } ; D \mid \epsilon \\ T &\rightarrow B C \mid \text{record } \{ D \} \\ B &\rightarrow \text{int} \mid \text{float} \\ C &\rightarrow \epsilon \mid [ \text{num} ] C \end{aligned}$$

The fragment of the above grammar that deals with basic and array types. Consider storage layout as well as types. Nonterminal  $D$  generates a sequence of declarations. Nonterminal  $T$  generates basic, array, or record types. Nonterminal  $B$  generates one of the basic types `int` and `float`. Nonterminal  $C$ , for "component," generates strings of zero or more integers, each integer surrounded by brackets. An array type consists of a basic type specified by  $B$ , followed by array components specified by nonterminal  $C$ . A record type (the second production for  $T$ ) is a sequence of declarations for the fields of the record, all surrounded by curly braces.

### 4. Storage Layout for Local Names

From the type of a name, we can determine the amount of storage that will be needed for the name at run time. At compile time, we can use these amounts to assign each name a relative address. The type and relative address are saved in the symbol-table entry for the name. Data of varying length, such as strings, or data whose size cannot be determined until run time, such as dynamic arrays, is handled by reserving a known fixed amount of storage for a pointer to the data.

#### Address Alignment

The storage layout for data objects is strongly influenced by the addressing constraints of the target machine. For example, instructions to add integers may expect integers to be *aligned*, that is, placed at certain positions in memory such as an address divisible by 4. Although an array of ten characters needs only enough bytes to hold ten characters, a compiler may therefore allocate 12 bytes—the next multiple of 4—leaving 2 bytes unused. Space left unused due to alignment considerations is referred to as *padding*. When space is at a premium, a compiler may *pack* data so that no padding is left; additional instructions may then need to be executed at run time to position packed data so that it can be operated on as if it were properly aligned.

Suppose that storage comes in blocks of contiguous bytes, where a byte is the smallest unit of addressable memory. The *width* of a type is the number of storage units needed for objects of that type. A basic type, such as a character, integer, or float, requires an integral number of bytes. For easy access, storage for aggregates such as arrays and classes is allocated in one contiguous block of bytes.

The translation scheme (SDT) computes types and their widths for basic and array types; The SDT uses synthesized attributes *type* and *width* for each nonterminal and two variables  $t$  and  $w$  to pass type and width information from a  $B$  node in a parse tree to the node for the production  $C \rightarrow \epsilon$ . In a syntax-directed definition,  $t$  and  $w$  would be inherited attributes for  $C$ .

The body of the T-production consists of nonterminal B, an action, and nonterminal C, which appears on the next line. The action between B and C sets *t* to B.type and *w* to B. width. If  $B \rightarrow \text{int}$  then B.type is set to integer and B.width is set to 4, the width of an integer. Similarly, if  $B \rightarrow \text{float}$  then B.type is float and B.width is 8, the width of a float.

The productions for C determine whether T generates a basic type or an array type. If  $C \rightarrow e$ , then *t* becomes C.type and *w* becomes C. width. Otherwise, C specifies an array component. The action for  $C \rightarrow [\text{num}] C_1$  forms C.type by applying the type constructor array to the operands num.value and C<sub>1</sub>.type.

$T \rightarrow$	$\begin{array}{c} B \\ C \end{array}$	$\{ t = B.type; w = B.width; \}$
$B \rightarrow$	<b>int</b>	$\{ B.type = integer; B.width = 4; \}$
$B \rightarrow$	<b>float</b>	$\{ B.type = float; B.width = 8; \}$
$C \rightarrow$	$\epsilon$	$\{ C.type = t; C.width = w; \}$
$C \rightarrow$	$[\text{num}] C_1$	$\{ \text{array}(\text{num.value}, C_1.type);$ $C.width = \text{num.value} \times C_1.width; \}$

Figure 6.15: Computing types and their widths

The width of an array is obtained by multiplying the width of an element by the number of elements in the array. If addresses of consecutive integers differ by 4, then address calculations for an array of integers will include multiplications by 4. Such multiplications provide opportunities for optimization, so it is helpful for the front end to make them explicit.

**Example** The parse tree for the type `int [2] [3]` is shown by dotted lines in Fig. 6.16. The solid lines show how the type and width are passed from B, down the chain of C's through variables *t* and *w*, and then back up the chain as synthesized attributes type and width. The variables *t* and *w* are assigned the values of B.type and B.width, respectively, before the subtree with the C nodes is examined. The values of *t* and *w* are used at the node for  $C \rightarrow e$  to start the evaluation of the synthesized attributes up the chain of C nodes.

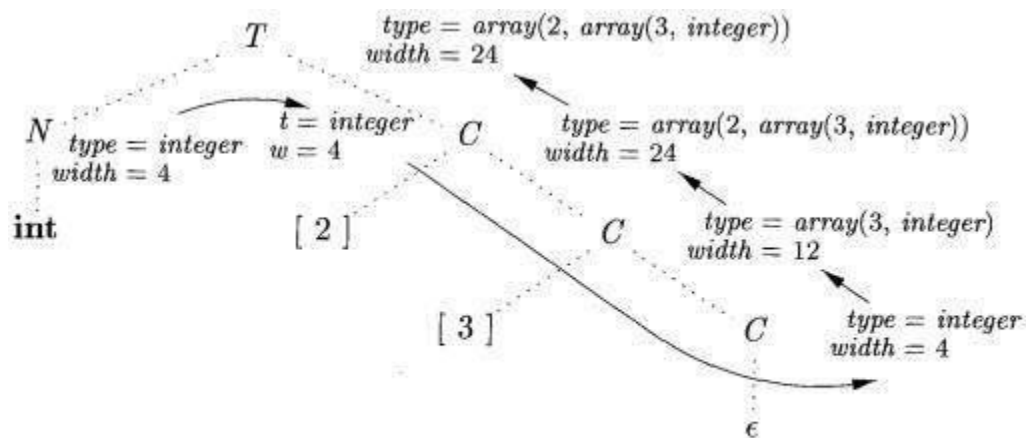


Figure 6.16: Syntax-directed translation of array types

## Translation of Expressions

- 1 Operations Within Expressions
- 2 Incremental Translation
- 3 Addressing Array Elements
- 4 Translation of Array References

### 1 Operations Within Expressions

The syntax-directed definition builds up the three-address code for an assignment statement  $S$  using attribute  $code$  for  $S$  and attributes  $addr$  and  $code$  for an expression  $E$ . Attributes  $S.code$  and  $E.code$  denote the three-address code for  $S$  and  $E$ , respectively. Attribute  $E.addr$  denotes the address that will hold the value of  $E$ .

PRODUCTION	SEMANTIC RULES
$S \rightarrow \text{id} = E ;$	$S.code = E.code \parallel$ $gen(top.get(\text{id.lexeme}) := E.addr)$
$E \rightarrow E_1 + E_2$	$E.addr = \text{new Temp}()$ $E.code = E_1.code \parallel E_2.code \parallel$ $gen(E.addr := E_1.addr + E_2.addr)$
$  - E_1$	$E.addr = \text{new Temp}()$ $E.code = E_1.code \parallel$ $gen(E.addr := \text{'minus'} E_1.addr)$
$  ( E_1 )$	$E.addr = E_1.addr$ $E.code = E_1.code$
$  \text{id}$	$E.addr = top.get(\text{id.lexeme})$ $E.code = ''$

Figure 6.19: Three-address code for expressions

**Example** The syntax-directed definition in Fig. 6.19 translates the assignment statement `a=b+-c;` into the TAC

```

t1 = minus c
t2 = b + t1
a = t2

```

### 2IncrementalTranslation

Code attributes can be long strings, so they are generated incrementally. In the incremental approach, *gen* not only constructs a three-address instruction, it appends the instruction to the sequence of instructions generated so far. The sequence may either be retained in memory for further processing, or it may be output incrementally. attribute *addr* represents the address of a node rather than a variable or constant.

```

S → id = E ; { gen( top.get(id.lexeme) '=' E.addr); }

E → E1 + E2 { E.addr = new Temp();
                  gen(E.addr '=' E1.addr '+' E2.addr); }

      | - E1    { E.addr = new Temp();
                  gen(E.addr '=' 'minus' E1.addr); }

      | ( E1 )  { E.addr = E1.addr; }

      | id       { E.addr = top.get(id.lexeme); }

```

Figure 6.20: Generating three-address code for expressions incrementally

### 3.AddressingArrayElements

Elements of arrays can be accessed quickly if the elements are stored in a block of consecutive location. Array can be one dimensional or two dimensional.

For one dimensional array:

```

A:array[low..high] of the i elements is at:
base+(i-low)*width=i*width +(base-low*width)

```

Multi-dimensional arrays:

- Row major or column major forms
  - Row major: a[1,1], a[1,2], a[1,3], a[2,1], a[2,2], a[2,3]
  - Column major: a[1,1], a[2,1], a[1,2], a[2,2], a[1, 3], a[2,3]
  - In row major form, the address of a[i1, i2] is
  - Base+((i1-low1)\*(high2-low2+1)+i2-low2)\*width

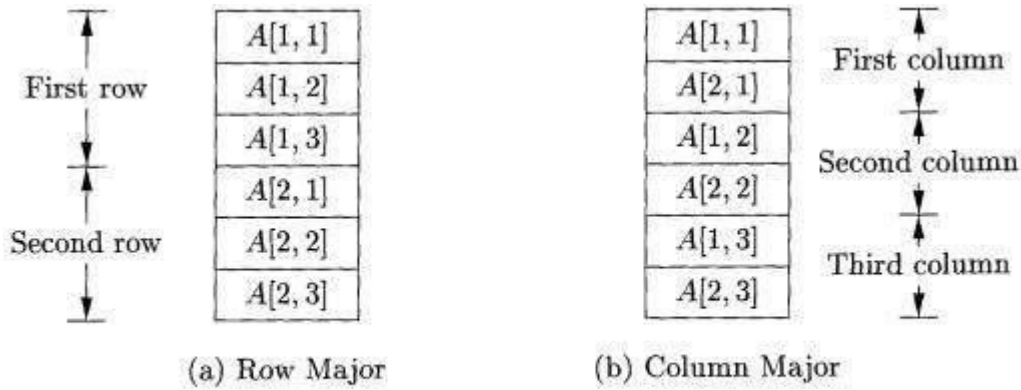


Figure 6.21: Layouts for a two-dimensional array.

#### 4 Translation of Array References

*L* generate an array name followed by a sequence of index expressions:

$$L \rightarrow L[E] \mid \text{id}[E]$$

Calculate addresses based on widths, using the formula rather than on numbers of elements. The translation scheme generates three-address code for expressions with array references. It consists of the productions and semantic actions together with productions involving nonterminal

```

S → id = E ;    { gen( top.get(id.lexeme) '=' E.addr); }
    | L = E ;    { gen(L.addr.base '[' L.addr ']' '=' E.addr); }

E → E1 + E2    { E.addr = new Temp();
                  gen(E.addr '=' E1.addr '+' E2.addr); }

    | id          { E.addr = top.get(id.lexeme); }

    | L           { E.addr = new Temp();
                  gen(E.addr '=' L.array.base '[' L.addr ']'); }

L → id [ E ]     { L.array = top.get(id.lexeme);
                  L.type = L.array.type.elem;
                  L.addr = new Temp();
                  gen(L.addr '=' E.addr '*' L.type.width); }

    | L1 [ E ]    { L.array = L1.array;
                  L.type = L1.type.elem;
                  t = new Temp();
                  L.addr = new Temp();
                  gen(t '=' E.addr '*' L.type.width);
                  gen(L.addr '=' L1.addr '+' t); }

```

Figure 6.22: Semantic actions for array references

## Type Checking

### 1 Rules for Type Checking

#### Type Conversions

### 3 Overloading of Functions and Operators

### 4 Type Inference and Polymorphic Functions

#### An Algorithm for Unification

Type checking a compiler needs to assign a type expression to each component of the source program. The compiler must then determine that these type expressions conform to a collection of logical rules that is called the type system for the source language.

### 1 Rules for Type Checking

Type checking can take on two forms: **synthesis and inference**. *Type synthesis* builds up the type of an expression from the types of its subexpressions. It requires names to be declared before they are used. The type of  $E_1 + E_2$  is defined in terms of the types of  $E_1$  and  $E_2$ . • A typical rule for type synthesis has the form

if  $f$  has type  $s \rightarrow t$  and  $x$  has type  $s$ ,  
then expression  $f(x)$  has type  $t$  (6.8)

**Type inference** determines the type of a language construct from the way it is used. Rule for type inference has the form

if  $f(x)$  is an expression,  
then for some  $\alpha$  and  $\beta$ ,  $f$  has type  $\alpha \rightarrow \beta$  and  $x$  has type  $\alpha$  (6.9)

## 2 Type Conversions

integers are converted to floats when necessary, using a unary operator (float). For example, the integer 2 is converted to a float in the code for the expression  $2 * 3.14$ :

```
t1 = (float) 2  
t2 = t1 * 3.14
```

Type conversion rules vary from language to language. The rules for Java in Fig. 6.25 distinguish between *widening* conversions, which are intended to preserve information, and *narrowing* conversions, which can lose information.

Conversion from one type to another is said to be *implicit* if it is done automatically by the compiler. Implicit type conversions, also called *coercions*,

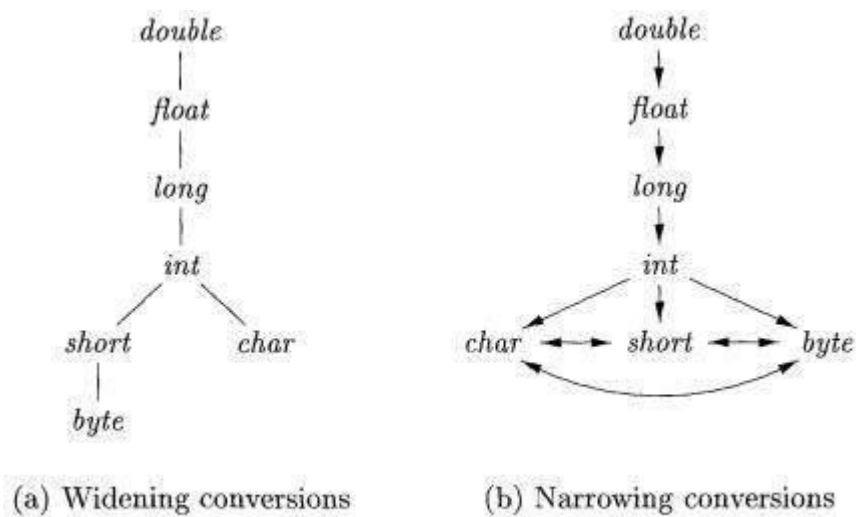


Figure 6.25: Conversions between primitive types in Java

### 3 Overloading of Functions and Operators

An *overloaded* symbol has different meanings depending on its context. The `+` operator in Java denotes either string concatenation or addition.

Type-synthesis rule for overloaded functions:

$$\begin{array}{l}
 \text{if } f \text{ can have type } s_i \rightarrow t_i, \text{ for } 1 \leq i \leq n, \text{ where } s_i \neq s_j \text{ for } i \neq j \\
 \text{and } x \text{ has type } s_k, \text{ for some } 1 \leq k \leq n \\
 \text{then expression } f(x) \text{ has type } t_k
 \end{array} \quad (6.10)$$

### 4 Type Inference and Polymorphic Functions

Type inference is useful for a language like ML, which is strongly typed, but does not require names to be declared before they are used. Type inference ensures that names are used consistently.

The term "polymorphic" refers to any code fragment that can be executed with arguments of different types.

The type of `length` can be described as, "for any type  $\alpha$ , `length` maps a list of elements of type  $\alpha$  to an integer."

```

fun length(x) =
    if null(x) then 0 else length(tl(x)) + 1;
  
```

Figure 6.28: ML program for the length of a list

The program fragment defines function `length` with one parameter  $x$ . The body of the function consists of a conditional expression. The predefined function `null` tests whether a list is empty, and the predefined function `tl` (short for "tail") returns the remainder of a list after the first element is removed.

5 AnAlgorithm forUnification

Unification is the problem of determining whether two expressions s and t can be made identicalby substituting expressions for the variables in s and t. Testing equality of expressions is a special caseof unification; if s and t have constants but no variables, then s and t unify if and only if they areidentical.so it can beusedto test structural equivalenceofcircular types .<sup>7</sup>

Graph-theoreticformulationofunification,wheretypesarerepresentedbygraphs.Typevariables are represented by leaves and type constructors are represented by interior nodes. Nodes aregroupedintoequiv-alenceclasses; iftwonodes areinthesameequivalenceclass,thenthe typeexpressions they represent must unify. Thus, all interior nodes in the same class must be for the sametypeconstructor, and their correspondingchildrenmust beequivalent.

Example6.18:Consider thetwotypeexpressions

$$\begin{aligned} &((\alpha_1 \rightarrow \alpha_2) \times list(\alpha_3)) \rightarrow list(\alpha_2) \\ &((\alpha_3 \rightarrow \alpha_4) \times list(\alpha_3)) \rightarrow \alpha_5 \end{aligned}$$

The following substitution *S* is the most general unifier for these expressions

<i>x</i>	<i>S</i> ( <i>x</i> )
$\alpha_1$	$\alpha_1$
$\alpha_2$	$\alpha_2$
$\alpha_3$	$\alpha_1$
$\alpha_4$	$\alpha_2$
$\alpha_5$	$list(\alpha_2)$

This substitution maps the two type expressions to the following expression

$$((\alpha_1 \rightarrow \alpha_2) \times list(\alpha_1)) \rightarrow list(\alpha_2)$$

```

boolean unify(Node m, Node n) {
    s = find(m); t = find(n);
    if ( s = t ) return true;
    else if ( nodes s and t represent the same basic type ) return true;
    else if ( s is an op-node with children s1 and s2 and
              t is an op-node with children t1 and t2 ) {
        union(s, t);
        return unify(s1, t1) and unify(s2, t2);
    }
    else if s or t represents a variable {
        union(s, t);
        return true;
    }
    else return false;
}

```

Figure 6.32: Unification algorithm.

The unification algorithm, uses the following two operations on nodes:

*find*(*n*) returns the representative node of the equivalence class currently containing node *n*.

*union*(*m*, *n*) merges the equivalence classes containing nodes *m* and *n*. If one of the representatives for the equivalence classes of *m* and *n* is a non-variable node, *union* makes that nonvariable node be the representative for the merged equivalence class; otherwise, *union* makes one or the other of the original representatives be the new representative. This asymmetry in the specification of *union* is important because a variable cannot be used as the representative for an equivalence class for an expression containing a type constructor or basic type. Otherwise, two inequivalent expressions may be unified through that variable.

## Control Flow

- 1 Boolean Expressions
- 2 Short-Circuit Code
- 3 Flow-of-Control Statements
- 4 Control-Flow Translation of Boolean

Expressions In programming languages, boolean expressions are often used to

1. **Alter the flow of control.** Boolean expressions are used as conditional expressions in statements that alter the flow of control. The value of such boolean expressions is implicit in a position reached in a program. For example, in `if(E)S`, the expression *E* must be true if statement *S* is reached.
2. **Compute logical values.** A boolean expression can represent *true* or *false* as values. Such boolean

expressions can be evaluated in analogy to arithmetic expressions using three-address instructions with logical operators.

## 1 Boolean Expressions

Boolean expressions are composed of the boolean operators (which we denote `&&`, `||`, and `!`, using the C convention for the operators AND, OR, and NOT, respectively) applied to elements that are boolean variables or relational expressions. Boolean expressions generated by the following grammar:

$$B \rightarrow B || B \mid B \&\& B \mid ! B \mid ( B ) \mid E \text{ rel } E \mid \text{true} \mid \text{false}$$

Given the expression  $B_1 || B_2$ , if we determine that  $B_1$  is true, then we can conclude that the entire expression is true without having to evaluate  $B_2$ . Similarly, given  $B_1 \&\& B_2$ , if  $B_1$  is false, then the entire expression is false.

## 2 Short-Circuit Code

In *short-circuit* (or *jumping*) code, the boolean operators `&&`, `||`, and `!` translate into jumps. The operators themselves do not appear in the code; instead, the value of a boolean expression is represented by a position in the code sequence.

**Example** The statement

```
if (x < 100 || x > 200 && x != y) x = 0;
```

might be translated into the code of Fig. 6.34. In this translation, the boolean expression is true if control reaches label  $L_2$ . If the expression is false, control goes immediately to  $L_u$  skipping  $L_2$  and the assignment  $x=0$ .

```

    if x < 100 goto L2
    if False x > 200 goto L1
    if False x != y goto L1
L2:  x = 0
L1:
```

Figure 6.34: Jumping code

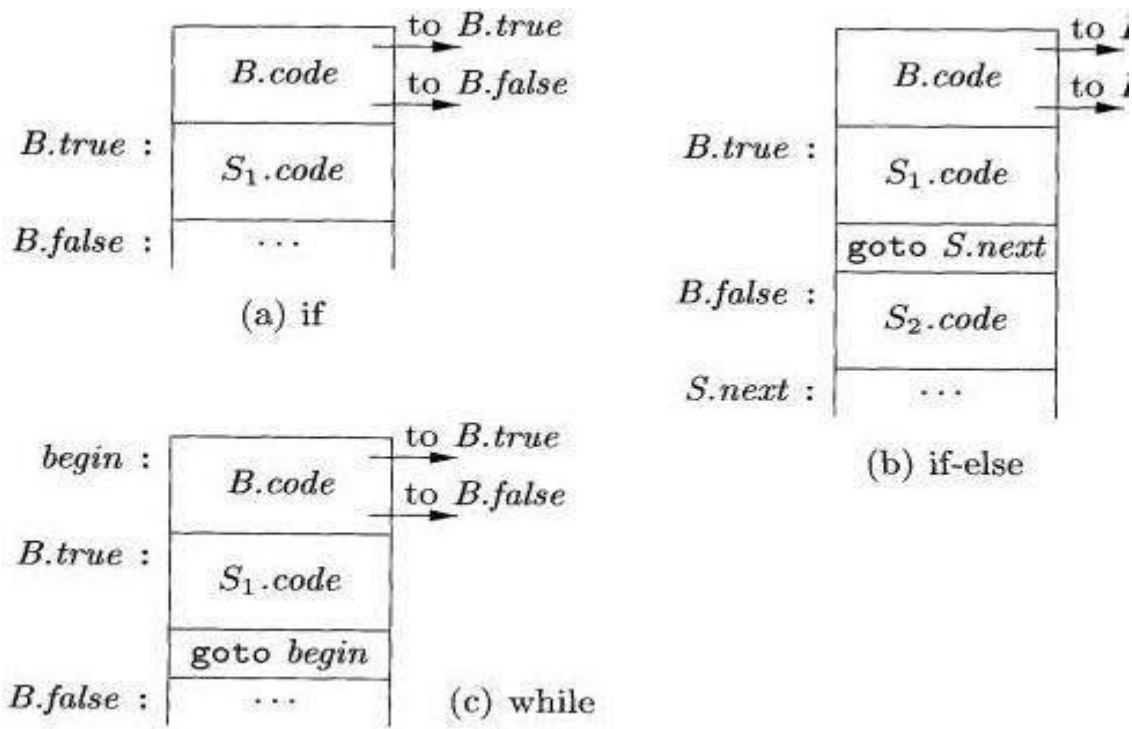
## 3 Flow-of-Control Statements

$$\begin{aligned} S &\rightarrow \text{if } ( B ) S_1 \\ S &\rightarrow \text{if } ( B ) S_1 \text{ else } S_2 \\ S &\rightarrow \text{while } ( B ) S_1 \end{aligned}$$

In these productions, nonterminal  $B$  represents a boolean expression and non-terminal  $S$  represents a statement.

*B* and *S* have a synthesized attribute *code*, which gives the translation into three-address instructions. we build up the translations *B.code* and *S.code* as strings, using syntax directed definitions.

The translation of *if*(*B*) *S*<sub>1</sub> consists of *B.code* followed by *S*<sub>1</sub>.*code*, as illustrated in Fig. 6.35(a). Within *B.code* are jumps based on the value of *B*. If *B* is true, control flows to the first instruction of *S*<sub>1</sub>.*code*, and if *B* is false, control flows to the instruction immediately following *S*<sub>1</sub>. *code*.



Code for if, if else, while statements

The syntax-directed definition in Fig. 6.36-6.37 produces three-address code for boolean expressions in the context of if-, if-else-, and while-statements.

PRODUCTION	SEMANTIC RULES
$P \rightarrow S$	$S.next = newlabel()$ $P.code = S.code \parallel label(S.next)$
$S \rightarrow \text{assign}$	$S.code = \text{assign}.code$
$S \rightarrow \text{if} ( B ) S_1$	$B.true = newlabel()$ $B.false = S_1.next = S.next$ $S.code = B.code \parallel label(B.true) \parallel S_1.code$
$S \rightarrow \text{if} ( B ) S_1 \text{ else } S_2$	$B.true = newlabel()$ $B.false = newlabel()$ $S_1.next = S_2.next = S.next$ $S.code = B.code$ $\quad \parallel label(B.true) \parallel S_1.code$ $\quad \parallel gen('goto' S.next)$ $\quad \parallel label(B.false) \parallel S_2.code$
$S \rightarrow \text{while} ( B ) S_1$	$begin = newlabel()$ $B.true = newlabel()$ $B.false = S.next$ $S_1.next = begin$ $S.code = label(begin) \parallel B.code$ $\quad \parallel label(B.true) \parallel S_1.code$ $\quad \parallel gen('goto' begin)$
$S \rightarrow S_1 S_2$	$S_1.next = newlabel()$ $S_2.next = S.next$ $S.code = S_1.code \parallel label(S_1.next) \parallel S_2.code$

Figure 6.36: Syntax-directed definition for flow-of-control statements.

4 Control-Flow Translation of Boolean Expressions

Boolean expression  $B$  is translated into three-address instructions that evaluate  $B$  using create label only when they are needed. Alternatively, unnecessary labels can be eliminated during a subsequent optimization phase.

PRODUCTION	SEMANTIC RULES
$B \rightarrow B_1 \parallel B_2$	$B_1.true = B.true$ $B_1.false = newlabel()$ $B_2.true = B.true$ $B_2.false = B.false$ $B.code = B_1.code \parallel label(B_1.false) \parallel B_2.code$
$B \rightarrow B_1 \&\& B_2$	$B_1.true = newlabel()$ $B_1.false = B.false$ $B_2.true = B.true$ $B_2.false = B.false$ $B.code = B_1.code \parallel label(B_1.true) \parallel B_2.code$
$B \rightarrow ! B_1$	$B_1.true = B.false$ $B_1.false = B.true$ $B.code = B_1.code$
$B \rightarrow E_1 \text{ rel } E_2$	$B.code = E_1.code \parallel E_2.code$ $\parallel gen('if' E_1.addr \text{ rel } op E_2.addr 'goto' B.true)$ $\parallel gen('goto' B.false)$
$B \rightarrow true$	$B.code = gen('goto' B.true)$
$B \rightarrow false$	$B.code = gen('goto' B.false)$

Figure 6.37: Generating three-address code for booleans

Backpatching

- 1 One-Pass Code Generation Using Backpatching
- 2 Backpatching for Boolean Expressions
- 3 Flow-of-Control Statements

1 One-Pass Code Generation Using Backpatching

The problem in generating three address codes in a single pass is that we may not know the labels that control must goto at the time jump statements are generated. So to get around this

problem a series of branching statements with the targets of the jumps temporarily left unspecified is generated. Back Patching is putting the address instead of labels when the proper label is determined.

To manipulate lists of jumps, Backpatching Algorithms perform three types of operations

1. *makelist(i)* creates a new list containing only *i*, an index into the array of instructions; *makelist* returns a pointer to the newly created list.
2. *merge(p1,p2)* concatenates the lists pointed to by *p1* and *p2*, and returns a pointer to the concatenated list.
3. *backpatch(p,i)* inserts *i* as the target label for each of the instructions on the list pointed to by *p*.

## 2 Backpatching for Boolean Expressions

Construct a translation scheme suitable for generating code for boolean expressions during bottom-up parsing. A marker nonterminal *M* in the grammar causes a semantic action to pick up, at appropriate times, the index of the next instruction to be generated. The grammar is as follows:

$$\begin{aligned}
 B &\rightarrow B_1 \ || \ M \ B_2 \ | \ B_1 \ \&\& \ M \ B_2 \ | \ ! \ B_1 \ | \ ( \ B_1 \ ) \ | \ E_1 \ \text{rel} \ E_2 \ | \ \text{true} \ | \ \text{false} \\
 M &\rightarrow \epsilon
 \end{aligned}$$

The translation scheme is in Fig. 6.43.

- |    |                                        |                                                                                                                                                                                                                                                                                                                |
|----|----------------------------------------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| 1) | $B \rightarrow B_1 \    \ M \ B_2$     | { <i>backpatch</i> ( <i>B</i> <sub>1</sub> . <i>false</i> list, <i>M</i> . <i>instr</i> );<br><i>B</i> . <i>true</i> list = <i>merge</i> ( <i>B</i> <sub>1</sub> . <i>true</i> list, <i>B</i> <sub>2</sub> . <i>true</i> list);<br><i>B</i> . <i>false</i> list = <i>B</i> <sub>2</sub> . <i>false</i> list; } |
| 2) | $B \rightarrow B_1 \ \&\& \ M \ B_2$   | { <i>backpatch</i> ( <i>B</i> <sub>1</sub> . <i>true</i> list, <i>M</i> . <i>instr</i> );<br><i>B</i> . <i>true</i> list = <i>B</i> <sub>2</sub> . <i>true</i> list;<br><i>B</i> . <i>false</i> list = <i>merge</i> ( <i>B</i> <sub>1</sub> . <i>false</i> list, <i>B</i> <sub>2</sub> . <i>false</i> list); } |
| 3) | $B \rightarrow ! \ B_1$                | { <i>B</i> . <i>true</i> list = <i>B</i> <sub>1</sub> . <i>false</i> list;<br><i>B</i> . <i>false</i> list = <i>B</i> <sub>1</sub> . <i>true</i> list; }                                                                                                                                                       |
| 4) | $B \rightarrow ( \ B_1 \ )$            | { <i>B</i> . <i>true</i> list = <i>B</i> <sub>1</sub> . <i>true</i> list;<br><i>B</i> . <i>false</i> list = <i>B</i> <sub>1</sub> . <i>false</i> list; }                                                                                                                                                       |
| 5) | $B \rightarrow E_1 \ \text{rel} \ E_2$ | { <i>B</i> . <i>true</i> list = <i>makelist</i> ( <i>nextinstr</i> );<br><i>B</i> . <i>false</i> list = <i>makelist</i> ( <i>nextinstr</i> + 1);<br><i>emit</i> ('if' <i>E</i> <sub>1</sub> . <i>addr</i> <i>rel.op</i> <i>E</i> <sub>2</sub> . <i>addr</i> 'goto -');<br><i>emit</i> ('goto -'); }            |
| 6) | $B \rightarrow \text{true}$            | { <i>B</i> . <i>true</i> list = <i>makelist</i> ( <i>nextinstr</i> );<br><i>emit</i> ('goto -'); }                                                                                                                                                                                                             |
| 7) | $B \rightarrow \text{false}$           | { <i>B</i> . <i>false</i> list = <i>makelist</i> ( <i>nextinstr</i> );<br><i>emit</i> ('goto -'); }                                                                                                                                                                                                            |
| 8) | $M \rightarrow \epsilon$               | { <i>M</i> . <i>instr</i> = <i>nextinstr</i> ; }                                                                                                                                                                                                                                                               |

Figure 6.43: Translation scheme for boolean expressions

Consider semantic action (1) for the production  $B \rightarrow B_1 \parallel M B_2$ . If  $Bx$  is true, then  $B$  is also true, so the jump on  $B_1$  true list become part of  $B$  true list. If  $B_1$  is false, however, we must next test  $B_2$ , so the target for the jumps  $B > i$  false list must be the beginning of the code generated for  $B_2$ . This target is obtained using the marker nonterminal  $M$ . That nonterminal produces, as a synthesized attribute  $M.i$ , the index of the next instruction, just before  $B_2$  code starts being generated.

**Example**  
Consider expression

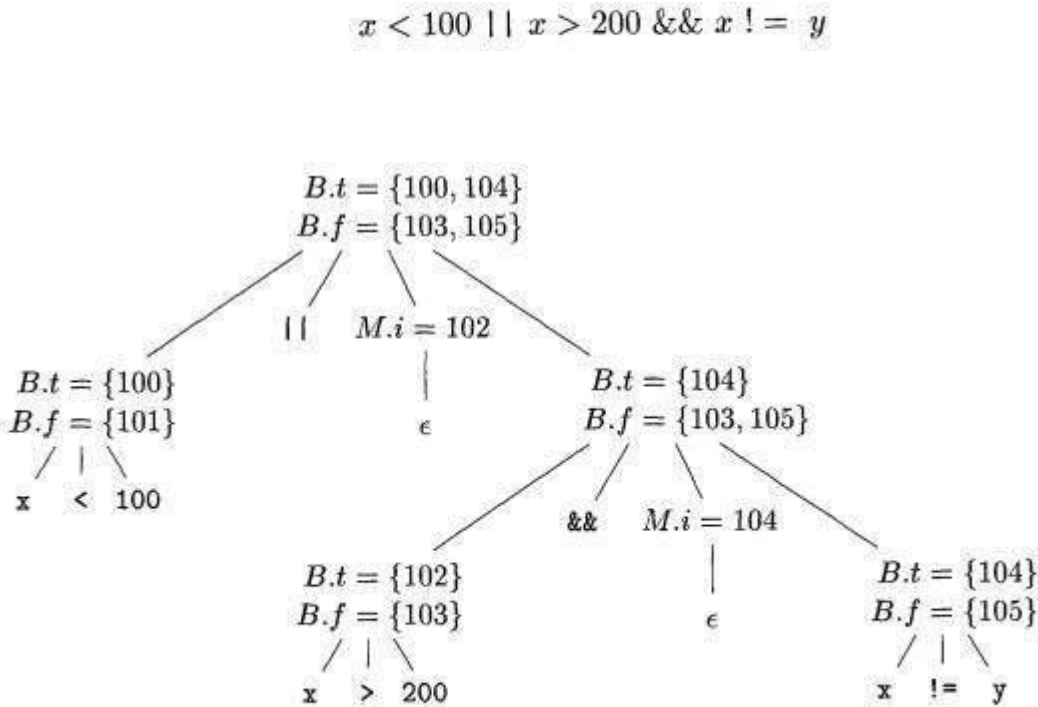


Figure 6.44: Annotated parse tree for  $x < 100 \parallel x > 200 \&\& x \neq y$

An annotated parse tree is shown in Fig. 6.44; attributes *truelist*, *falselist*, and *instr* are represented by their initial letters. The actions are performed during a depth-first traversal of the tree. Since all actions appear at the ends of right sides, they can be performed in conjunction with reductions during a bottom-up parse. In response to the reduction of  $x < 100$  to  $B$  by production (5), the two instructions

```

100:  if x < 100 goto -
101:  goto -

```

are generated. (start instruction numbers at 100.) The marker nonterminal  $M$  in the production

$$B \rightarrow B_1 \parallel M B_2$$

records the value of next instr, which at this time is 102.

The reduction of  $x > 200$  to  $B$  by production (5) generates the instructions

```

102:  if x > 200 goto -
103:  goto -

```

The subexpression  $x > 200$  corresponds to  $B_1$  in the production

$$B \rightarrow B_1 \ \&\& \ M \ B_2$$

The marker nonterminal  $M$  records the current value of *nextinstr*, which is

now  $\text{Reducing } x \neq y \text{ into } B$  by production (5) generates

```

104:  if x != y goto -
105:  goto -

```

We now reduce by  $B \rightarrow B_1 \ \&\& \ M \ B_2$ . The corresponding semantic action calls `backpatch(B1.truelist, M.instr)` to bind the true exit of  $B_1$  to the first instruction of  $B_2$ . Since  $B_1.\text{truelist}$  is  $\{102\}$  and  $M.\text{instr}$  is 104, this call to `backpatch` fills in 104 in instruction 102. The six instructions generated so far are thus as shown in Fig. 6.45(a).

The semantic action associated with the final reduction by  $B \rightarrow B_1 \ || \ M \ B_2$  calls `backpatch(\{101\}, 102)` which leaves the instructions as in Fig

The entire expression is true if and only if the gotos of instructions 100 or 104 are reached, and is false if and only if the gotos of instructions 103 or 105 are reached. These instructions will have their targets filled in later in the compilation, when it is seen what must be done depending on the truth or falsehood

```

100:  if x < 100 goto -
101:  goto -
102:  if x > 200 goto 104
103:  goto -
104:  if x != y goto -
105:  goto -

```

(a) After backpatching 104 into instruction 102.

```

100:  if x < 100 goto -
101:  goto 102
102:  if y > 200 goto 104
103:  goto -
104:  if x != y goto -
105:  goto -

```

(b) After backpatching 102 into instruction 101.

Figure 6.45: Steps in the backpatch process

of the expression. as

### 3 Flow-of-Control Statements

use backpatching to translate flow-of-control statements in one pass.

$$S \rightarrow \text{if}(B) S \mid \text{if}(B) S \text{ else } S \mid \text{while}(B) S \mid \{L\} \mid A ;$$

$$L \rightarrow L S \mid S$$

The translation scheme in Fig. 6.46 maintains lists of jumps that are filled in when their targets are found.

- 1)  $S \rightarrow \text{if}(B) M S_1$  {  $\text{backpatch}(B.\text{truelist}, M.\text{instr});$   
 $S.\text{nextlist} = \text{merge}(B.\text{falselist}, S_1.\text{nextlist});$  }
- 2)  $S \rightarrow \text{if}(B) M_1 S_1 N \text{ else } M_2 S_2$   
{  $\text{backpatch}(B.\text{truelist}, M_1.\text{instr});$   
 $\text{backpatch}(B.\text{falselist}, M_2.\text{instr});$   
 $\text{temp} = \text{merge}(S_1.\text{nextlist}, N.\text{nextlist});$   
 $S.\text{nextlist} = \text{merge}(\text{temp}, S_2.\text{nextlist});$  }
- 3)  $S \rightarrow \text{while } M_1 (B) M_2 S_1$   
{  $\text{backpatch}(S_1.\text{nextlist}, M_1.\text{instr});$   
 $\text{backpatch}(B.\text{truelist}, M_2.\text{instr});$   
 $S.\text{nextlist} = B.\text{falselist};$   
 $\text{emit}(\text{'goto' } M_1.\text{instr});$  }
- 4)  $S \rightarrow \{L\}$  {  $S.\text{nextlist} = L.\text{nextlist};$  }
- 5)  $S \rightarrow A ;$  {  $S.\text{nextlist} = \text{null};$  }
- 6)  $M \rightarrow \epsilon$  {  $M.\text{instr} = \text{nextinstr};$  }
- 7)  $N \rightarrow \epsilon$  {  $N.\text{nextlist} = \text{makelist}(\text{nextinstr});$   
 $\text{emit}(\text{'goto' } -);$  }
- 8)  $L \rightarrow L_1 M S$  {  $\text{backpatch}(L_1.\text{nextlist}, M.\text{instr});$   
 $L.\text{nextlist} = S.\text{nextlist};$  }
- 9)  $L \rightarrow S$  {  $L.\text{nextlist} = S.\text{nextlist};$  }

Figure 6.46: Translation of statements

Backpatch the jumps when B is true to the instruction  $M_i.\text{instr}$ ; the latter is the beginning of the code for  $S_i$ . Similarly, we backpatch jumps when B is false to go to the beginning of the code for  $S_2$ . The list  $S.\text{nextlist}$  includes all jumps out of  $S_i$  and  $S_2$ , as well as the jump generated by N. (Variable  $\text{temp}$  is a temporary that is used only for merging lists.)

Semantic actions (8) and (9) handle sequences of statements. In

$$L \rightarrow L_1 M S$$

the instruction following the code for  $L_1$  in order of execution is the beginning of  $S$ . Thus the  $L_1$ .nextlist list is backpatched to the beginning of the code for  $S$ , which is given by  $M$ .instr. In  $L \rightarrow S$ ,  $L$ .nextlist is the same as  $S$ .nextlist.

Note that no new instructions are generated anywhere in these semantic rules, except for rules (3) and (7). All other code is generated by the semantic actions associated with assignment-statements and expressions. The flow of control causes the proper backpatching so that the assignments and boolean expression evaluations will connect properly.